

Uplink Design

$$\left(\frac{C}{N_0}\right)_{\text{uplink in db Hz}} = 10\log P_T G_T - 20\text{Log}\left(\frac{4\pi d}{\lambda}\right) + 10\log\frac{G}{T} \\ - 10\text{Log}L_A - 10\text{Log}K - BO_i$$

COMPLETE LINK DESIGN

- TWO EARTH STATION AND SATELLITE
- UP LINK AND DOWN LINK
- (UPLINK, SATELLITE TRANSPONDER, DOWN LINK
- UPLINK $(C/N_o)_u$ AT TRANSPONDER INPUT
- DOWNLINK $(C/N_o)_d$

Complete link design cont---

$$C = \frac{C_U G_s G_T G_R}{L}$$

C - Carrier Signal At Receiving Earth Station

CU - SIGNAL POWER AT THE SATELLITE TRANSPONDER INPUT

G_s – SATELLITE TRANSPONDER GAIN

G_T- GAIN OF THE SATELLITE TRANSMITTING ANTENNA

G_R – GAIN OF THE RECEIVING ANTENNA

L – LOSSES ON THE DOWN LINK

NOISE POWER SPECTRAL DENSITY AT THE INPUT OF THE RECEIVING ANTENNA

$$N_0 = N_{0D} + \frac{N_{0U} G_s G_T G_R}{L}$$

N_0 IS NOISE POWER SPECTRAL DENSITY AT THE INPUT OF THE RECEIVING STATION

N_{0U} IS NOISE POWER SPECTRAL DENSITY AT THE TRANSPONDER INPUT

$$\frac{C}{N_0} = \frac{\frac{C_U G_s G_T G_R}{L}}{N_{0D} + \frac{N_{0U} G_s G_T G_R}{L}}$$

$$= \frac{C_U}{N_{0U} + \frac{N_{0D} L}{G_s G_T G_R}}$$

TRANSPONDER HAS A BAND WIDTH B AND RADIATES A CONSTANT POWER P_T AND ITS GAIN G_S

$$G_S = \frac{P_T}{C_U + N_{0U} * B}$$

FOR DOWN LINK SIGNAL POWER CD

$$C_D = \frac{P_T G_T G_R}{L}$$

THUS C/No

$$\begin{aligned} \frac{C}{N_0} &= \frac{C_U}{N_{0U} + \frac{N_{0D} \cdot L (C_U + N_{0U} * B)}{P_T \cdot G_T G_R}} \\ &= \frac{C_U}{N_{0U} + \frac{N_{0D} \cdot (C_U + N_{0U} * B)}{C_D}} \end{aligned}$$

$$\frac{C}{N_0} = \frac{\frac{C_U * C_D}{N_{0U} * N_{0D}}}{\frac{N_{0U} * C_D + N_{0D} * (C_U + N_{0U} * B)}{N_{0U} * N_{0D}}}$$

$$= \frac{\left(\frac{C}{N_0}\right)_u * \left(\frac{C}{N_0}\right)_D}{\left(\frac{C}{N_0}\right)_u + \left(\frac{C}{N_0}\right)_D + B}$$

$$\left(\frac{C}{N_0}\right)_T^{-1} = \left(\frac{C}{N_0}\right)_u^{-1} + \left(\frac{C}{N_0}\right)_D^{-1} \rightarrow B \leq \left(\frac{C}{N_0}\right)_u \& \left(\frac{C}{N_0}\right)_D$$

Complete link design

- Effect of interfering signals
- I is noise power involved with the interfering signals under the band width of the desired carrier than , the net C/N ratio (for uplink)

$$\left(\frac{C}{N}\right)_{netuplink} = \left[\left(\frac{C}{N}\right)_U^{-1} + \left(\frac{C}{I}\right)_U^{-1} \right]$$

$$\left(\frac{\mathbf{C}}{\mathbf{N}}\right)_{net\ downlink} = \left[\left(\frac{\mathbf{C}}{\mathbf{N}}\right)_D^{-1} + \left(\frac{\mathbf{C}}{\mathbf{I}}\right)_D^{-1} \right]^{-1}$$

$$\left(\frac{\mathbf{C}}{\mathbf{N}}\right)_{net} = \left[\left(\frac{\mathbf{C}}{\mathbf{N}}\right)_{Net\ uplink} + \left(\frac{\mathbf{C}}{\mathbf{N}}\right)_{net\ downlink} \right]^{-1}$$

$$= \left[\left(\frac{\mathbf{C}}{\mathbf{N}}\right)_u^{-1} + \left(\frac{\mathbf{C}}{\mathbf{I}}\right)_u^{-1} + \left(\frac{\mathbf{C}}{\mathbf{N}}\right)_D^{-1} + \left(\frac{\mathbf{C}}{\mathbf{I}}\right)_D^{-1} \right]^{-1}$$

$$\left[\left(\frac{\mathbf{C}}{\mathbf{N}}\right)^{-1} + \left(\frac{\mathbf{C}}{\mathbf{I}}\right)^{-1} \right]^{-1}$$

$$\left(\frac{\mathbf{C}}{\mathbf{I}}\right)^{-1} = \left(\frac{\mathbf{C}}{\mathbf{I}}\right)_u^{-1} + \left(\frac{\mathbf{C}}{\mathbf{I}}\right)_D^{-1}$$

Complete link design contt---

- C/N CARRIER TO NOISE OF OVERALL LINK
- C/I CARRIER TO INTERFERENCE RATIO OF OVERALL LINK
- $C/I > C/N$ SATELLITE LINK IS NOISE DOMINANT
- $C/I < C/N$ SATELLITE IS CALLED INTERFERENCE DOMINANT
- FOR A TYPICAL FM DEMODULATOR S/N AFTER DEMODULATOR
- $(S/N)_{\text{OUTPUT}} = (C/N)_{\text{in}} + \text{FM IMPROVEMENT}$

Earth station parameter

$$\frac{C}{N_0} = \frac{P_T G_T G_R}{K T_S} \left(\frac{\lambda}{4 \pi d} \right)^2 \frac{1}{L_A}$$

- d is the range between transmitting and receiving antenna

$$G = \eta \left(\frac{4 \pi D}{\lambda} \right)^2$$
$$G = \frac{\eta 4 \pi^2 70^2}{\theta_{3 \text{ dB}}^2}$$

Contd---

- η antenna efficiency
- $(\theta_{3dB})_{sat}$ satellite antenna beam width
- D_{ES} is earth station diameter

$$G = \eta \left(\frac{4 \pi D}{\lambda} \right)^2$$
$$G = \frac{\eta 4 \pi^2 70^2}{\theta_{3dB}^2}$$

Earth station parameter

$$\frac{C}{N_0} = \frac{P_T}{L_A N_0} \eta_T \eta_R - \frac{\pi^2 70^2 D_{ES}^2}{d^2 (\theta_{3db})_{sat}^2}$$

FOR FIXED EARTH STATION

$$\frac{C}{N_0} = \frac{P_T}{L_A N_0} \eta_T \eta_R \frac{\pi^2 C^2 70^2}{(4d)^2 (\theta_{3db})_{sat}^2 (\theta_{3db})_{ES}^2 \cdot f^2}$$

$$\frac{C}{N_0} = \frac{P_T}{L_A N_0} \eta_T \eta_R \left(\frac{\pi D_{sat} D_{ES}}{4dC} \right)^2 f^2$$

Assignment 6

- Derive the expression for C/N ratio of satellite link design.